

Формули по статистика

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

| Доверителен интервал | Предположения | Интервал |
|----------------------------------|---|---|
| За μ | $N(\mu, \sigma^2)$ или n голямо σ^2 известно | $\left[\bar{x} - z_{\alpha/2} \frac{\sigma}{\sqrt{n}}, \bar{x} + z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \right]$ |
| За μ | $N(\mu, \sigma^2)$ σ^2 неизвестно | $\left[\bar{x} - t_{\frac{\alpha}{2}, n-1} \frac{S}{\sqrt{n}}, \bar{x} + t_{\frac{\alpha}{2}, n-1} \frac{S}{\sqrt{n}} \right]$ |
| Хипотези | Предположения | Критична област |
| $H_1: \mu > c$ | $N(\mu, \sigma^2)$ или n голямо σ^2 известно | $z = \frac{\bar{x} - c}{\sigma} \sqrt{n} \geq z_\alpha$ |
| $H_1: \mu > c$ | $N(\mu, \sigma^2)$ σ^2 неизвестно | $t = \frac{\bar{x} - c}{S} \sqrt{n} \geq t_{\alpha, n-1}$ |
| $H_1: \mu_X - \mu_Y > c$ | $N(\mu_X, \sigma^2_X) \quad N(\mu_Y, \sigma^2_Y)$ σ^2_X, σ^2_Y известни | $z = \frac{\bar{x} - \bar{y} - c}{\sqrt{\frac{\sigma^2_X}{n} + \frac{\sigma^2_Y}{m}}} \geq z_\alpha$ |
| $H_1: \mu_X - \mu_Y > c$ | Големи обеми, Неизвестни дисперсии | $t = \frac{\bar{x} - \bar{y} - c}{\sqrt{\frac{s^2_X}{n} + \frac{s^2_Y}{m}}} \geq z_\alpha$ |
| $H_1: \mu_X - \mu_Y > c$ | $N(\mu_X, \sigma^2_X) \quad N(\mu_Y, \sigma^2_Y)$ $\sigma^2_X = \sigma^2_Y$ неизвестни | $t = \frac{\bar{x} - \bar{y} - c}{\sqrt{s_p^2 (\frac{1}{n} + \frac{1}{m})}} \geq t_{\alpha, n+m-2}$ $s_p^2 = \frac{(n-1)s^2_X + (m-1)s^2_Y}{n+m-2}$ |
| $H_1: \mu_D = \mu_X - \mu_Y > c$ | X и Y нормални, зависими извадки | $t = \frac{\bar{d} - c}{s_d} \sqrt{n} \geq t_{\alpha, n-1}$ |
| $H_1: p > p_0$ | Bi(n, p) n голямо | $z = \frac{\frac{x}{n} - p_0}{\sqrt{p_0(1-p_0)}} \sqrt{n} \geq z_\alpha$ |
| $H_1: p_1 - p_2 > D_0$ | $Bi(n, p_1) \quad Bi(m, p_2)$ n, m големи | $z = \frac{(\hat{p}_1 - \hat{p}_2) - D_0}{\sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n-1} + \frac{\hat{p}_2(1-\hat{p}_2)}{m-1}}} \geq z_\alpha$ $\hat{p}_1 = \frac{x}{n} \quad \hat{p}_2 = \frac{y}{m}$ |